

U.G. 1st Semester Examination - 2021

PHYSICS

[HONOURS]

Course Code : PHY-H-CC-P-01

(Mathematical Physics-I)

[PRACTICAL]

Full Marks : 20

Time : 2 Hours

Use any of the programming languages python/ Fortran/Matlab/C/C++ to solve the following physical problems.

Answer any **four** questions: $5 \times 4 = 20$

- Given some data: 87, 91, 85, 75, 28, 122, 66 and 56. Find the (arithmetic) mean and r.m.s. (root mean square) value of the variable.
- Write a computer program to compute $n!$, where $n=10$.
- Find the value of π from the infinite series: up to the 6th decimal of accuracy.

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} + \dots$$

[Turn over]

- Starting with $u_1 = 1, u_2 = 1$, generate 20 Fibonacci numbers with the sequence $u_{n+1} = u_n + u_{n-1}$ and then calculate the following series sum: $S = \sum_{n=1}^{20} \frac{1}{u_n^2}$.
- Using the bisection method find a root of the following equation $x \sin x - 1 = 0$ in the interval $[0, 2]$.
- You have a set of data points given in the tabular form in the following:

x	5	10	15	20	25	30
y	45	105	174	259	364	496

Find out the value of y for $x = 18$ using Newton's forward difference formula.

- Write a computer program to find the trace, $\text{Tr}(A)$ of the following matrix:

$$A = \begin{pmatrix} 3 & 4 & 8 \\ 5 & 9 & 2 \\ 1 & 6 & 0 \end{pmatrix}$$

- Compute the value of π from the formula:

$$\frac{\pi}{4} = \int_0^1 \frac{dx}{1+x^2}$$

Use composite Simpson's 1/3 rule to evaluate with an accuracy of the order of 10^{-5} .

9. Write a program to solve the differential equation for the damped harmonic motion: (code may be written following Euler/Runge-Kutta 2nd order/Runge-Kutta 4th Order method)

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 0, \text{ with } y(0) = 0, x(0) = 0, y'(0) = 1.0$$

10. The temperature of a well-stirred liquid by the isothermal heating coil is given by the equation:

$$\frac{d\theta}{dt} = K(100 - \theta), \text{ where } K \text{ is a constant of the system.}$$

Write a computer program to solve the equation by any suitable method to find θ at $t = 1.0$ sec for $K=2.5$.

Initial condition: $\theta = 25^\circ\text{C}$ at $t = 0$ sec.
